

**MID SEMESTER EXAM-2018 SOLUTIONS**  
**5th SEMESTER**  
**Analog Electronics**

Ques. 1(a)

Transconductance ( $g_m$ )  $\rightarrow$  The transconductance of BJT is defined as the rate of change of collector current ( $I_c$ ) with respect to input voltage ( ~~$V_{BE}$~~  i.e. base to emitter voltage ( $V_{BE}$ )).

$$I_c = I_S \exp\left(\frac{V_{BE}}{V_T}\right) = I_S \exp\left(\frac{V_{BE} + V_{BE}}{V_T}\right)$$

$$= I_S \exp\left(\frac{V_{BE}}{V_T}\right) \exp\left(\frac{V_{BE}}{V_T}\right)$$

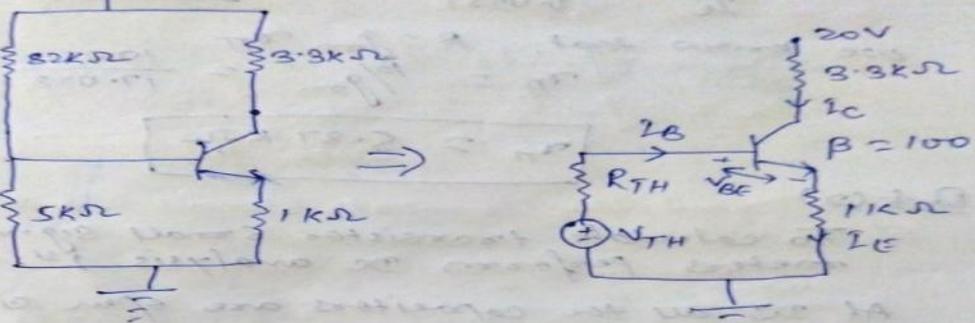
$$= I_c \exp\left(\frac{V_{BE}}{V_T}\right)$$

$$g_m = \frac{\partial I_c}{\partial V_{BE}} = \frac{I_c}{V_T}$$

Output resistance ( $r_o$ ) - The Early effect, causes the collector current to depend not only on  $V_{BE}$  but also on  $V_{CE}$ . The output resistance  $r_o$  is given by,

$$r_o = \frac{V_A + V_{CE}}{I_c} \approx \frac{V_A}{I_c}$$

DC analysis  $\rightarrow$  20V  
Ques. (1)-(b)



where,  $V_{TH} = \frac{5}{5+82} \times 20 = 1.15V$

$R_{TH} = 82 || 5 = 4.71k\Omega$

Apply KVL in base-emitter loop.

$$V_{TH} - I_B R_{TH} - V_{BE} - I_E R_E = 0$$

since,  $I_E = (1+\beta) I_B$

$$I_B (R_{TH} + (1+\beta) R_E) = V_{TH} - V_{BE}$$

$$\therefore I_B = \frac{1.15 - 0.7}{4.71 + 101 \times 1} = \frac{0.45}{105.71} = 4.257 \mu A$$

$$I_C = \beta I_B = 4.257 \times 100 = 0.4257 mA$$

$$g_m = \frac{I_C}{V_T} = 17.028 mS$$

$$r_o = \frac{V_A}{I_c} = \frac{100}{0.4257} \text{ k}\Omega \approx \underline{\underline{235 \text{ k}\Omega}} \quad (3)$$

we know that,  $\beta = g_m r_{\pi}$

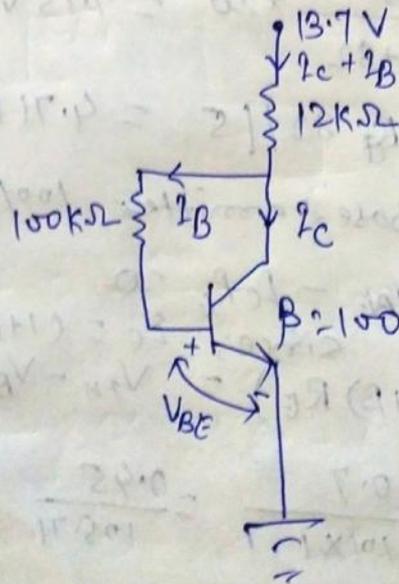
$$r_{\pi} = \beta / g_m = \frac{100}{17.028} \text{ k}\Omega$$

$$r_{\pi} = 5.87 \text{ k}\Omega$$

Ques. (2)

To calculate transistor small signal parameters perform DC analysis 1st.

At DC, all the capacitors are open circuited thus, circuit becomes



Apply KVL from 13.7V to ground through base-emitter loop.

$$13.7 - 12(I_C + I_B) - 100 I_B - V_{BE} = 0$$

$$\text{Since } I_C = \beta I_B = 100 I_B$$

$$\therefore I_B = \frac{13.7 - 0.7}{100 + 12 \times 100} = \frac{13}{1312} \text{ mA}$$

$$\approx 10 \mu\text{A}$$

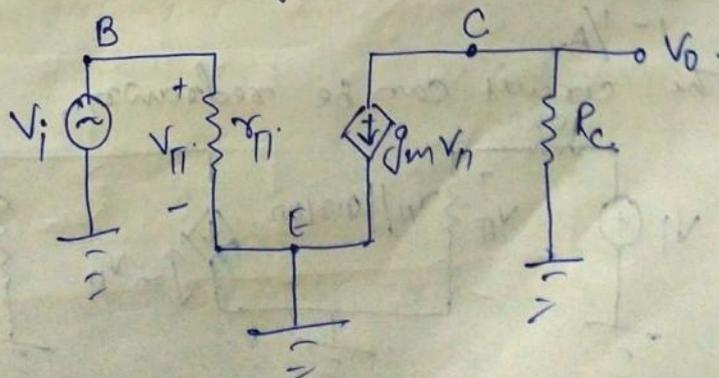
$$I_C = \beta I_B = 1 \text{ mA}$$

$$g_{m0} = \frac{I_C}{V_T} = \frac{1 \text{ mA}}{25 \text{ mV}} = 1/25 \text{ A/V}$$

$$r_{\pi} = \beta / g_{m0} = \frac{100}{1/25} = 2.5 \text{ k}\Omega$$

~~Now, draw the small signal model of BJT for voltage gain.~~

Since a feedback resistor is connected between collector and base, so this circuit can be solved by using miller's theorem. For that 1st we ~~have~~ would have to calculate transistor internal gain.



$$V_o = -g_m V_{\pi} R_c$$

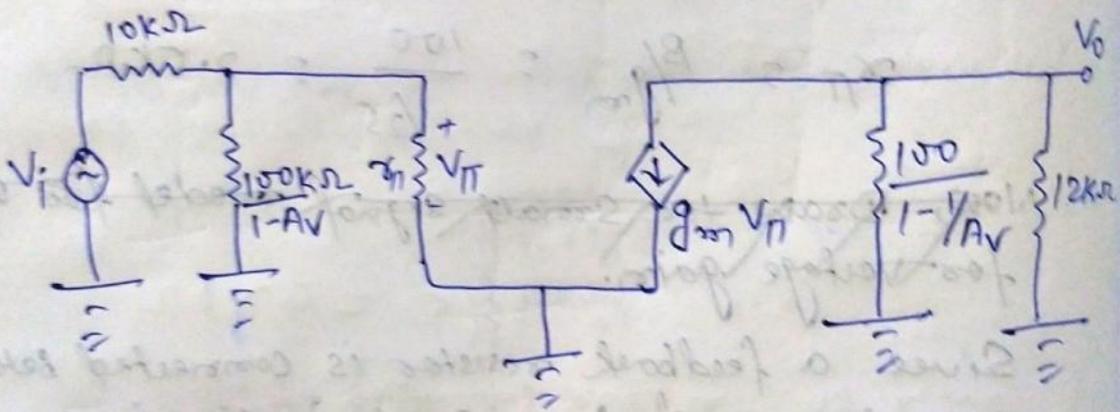
and  $V_{\pi} = V_i$

$$\therefore V_o = -g_m R_c V_i$$

$$A_v = -g_m R_c = -\frac{1}{25} \times 12 \times 1000$$

$$= -480$$

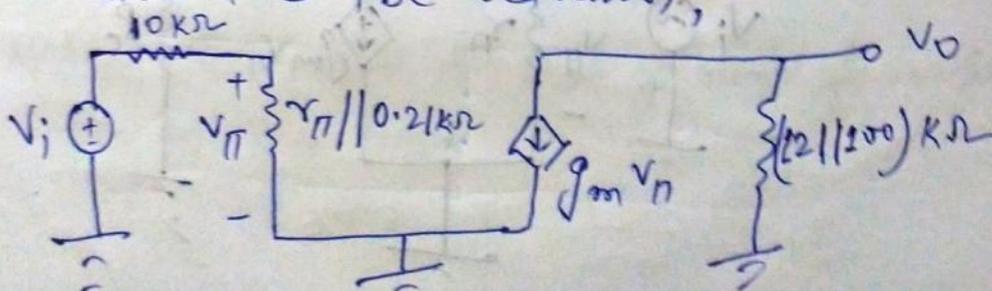
Now Draw the complete small signal model of transistor.



$$\frac{100}{1 - A_v} = \frac{100}{1 + 480} = 0.21 \text{ k}\Omega$$

$$\frac{100}{1 - 1/A_v} \approx 100 \text{ k}\Omega$$

The circuit can be redrawn,



$$\therefore V_o = -g_m V_{\pi} (12 \parallel 100) \quad \text{--- (i)}$$

$$V_o = -g_m V_{\pi} (10.71 \text{ k}\Omega) \quad \text{--- (ii)}$$

Now,  $r_{\pi} \parallel 0.2 \text{ k}\Omega = \frac{2.5 \times 0.2}{2.5 + 0.2} = 0.194 \text{ k}\Omega$

Let  $R_i = r_{\pi} \parallel 0.2 \text{ k}\Omega = 0.194 \text{ k}\Omega$

$$\therefore V_{\pi} = \frac{0.194}{10 + 0.194} V_i = 0.019 V_i$$

put  $V_{\pi}$  in eq<sup>n</sup> (i)

$$V_o = -g_m (10.71 \text{ k}\Omega) \times (0.019) V_i$$

$$\therefore A_v' = -\frac{1}{25} \times 10.71 \times 1000 \times 0.019$$

$$A_v' = -8.14$$

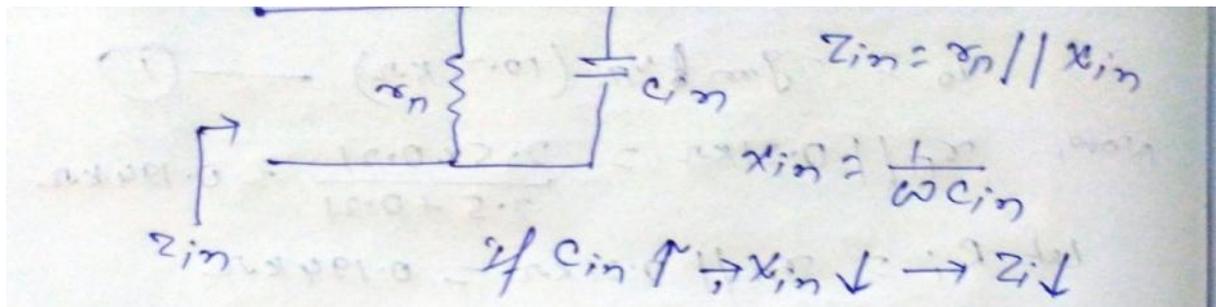
Qns: (3) (a)

(i) Due to increase in input capacitance, the Bandwidth of CE configuration decreases.

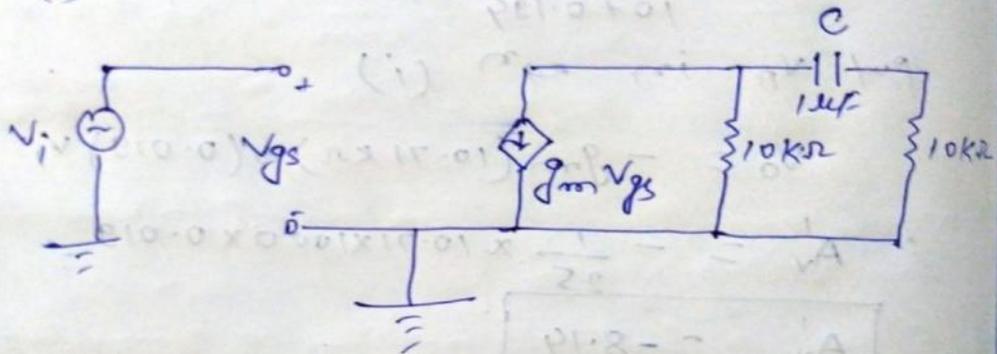
$$B.W. \approx f_H \approx \frac{1}{2\pi C_{in} (R_s \parallel R_i)}$$

Therefore, CE configuration is not suitable in wideband Amplifiers.

(ii) Input impedance of CE configuration decreases at high frequencies.



Ques. (3) (b)

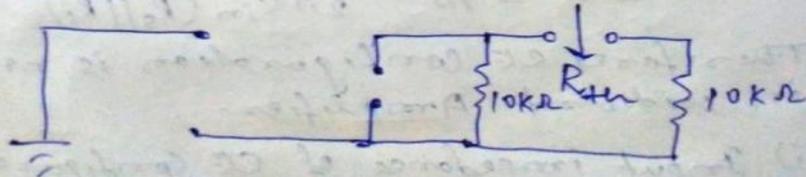


To calculate lower cut-off frequency  $V_i = 0$

Since,  $V_i = 0$ , so,  $V_{gs} = V_i = 0$

Thus,  $g_m V_{gs} = 0$

~~open~~ so, circuit reduce to



$$R_{th} = R_D + R_L = (10 + 10) = 20 \text{ k}\Omega$$

$$f_L = \frac{1}{2\pi C R_{th}} = \frac{1}{2\pi \times 10^{-6} \times 20 \times 10^3}$$

$$= \frac{25}{\pi} \text{ Hz}$$

$$\therefore f_L = 7.957 \text{ Hz}$$

**Ques. 4 (a)**

a.  $A_f = A/(1 + A) = -100/(1 + (-0.1)(-100))$

$= -100/11 = -9.09$

$Z_{if} = Z_i (1 + A) = 10 \text{ k} \cdot (11) = 110 \text{ k}$

$Z_{of} = Z_o / (1 + A) = 20 * 10^3 / 11 = 1.82 \text{ k}$

b.  $A_f = A/(1 + A) = -100/(1 + (-0.5)(-100))$

$= -100/51 = -1.96$

$Z_{if} = Z_i (1 + A) = 10 \text{ k} \cdot (51) = 510 \text{ k}$

$Z_{of} = Z_o / (1 + A) = 20 * 10^3 / 51 = 392.16$

Ques. 4 (b)

Feedback Topologies ↓	Input impedance ( $Z_i$ )	output impedance ( $Z_o$ )
a) Voltage Series	Increases	Decreases
(b) Voltage Shunt	Decreases	"
(c) Current Series	Increases	Increases
(d) Current Shunt	Decreases	"

**Ques. 5**

a. For the emitter-follower configuration, the loaded gain is

$$V_{o1} = \frac{Z_{i2}}{Z_{i2} + Z_{o1}} A_{vNL} V_{i1} = \frac{26}{26+12} \times 1 \times V_{i1} = 0.684 V_{i1}$$

Therefore,  $A_{v1} = 0.684$

For the common base configuration,

$$V_{o2} = \frac{R_L}{R_L + R_{o2}} A_{vNL} V_{i2} = \frac{8.2}{8.2+5.1} \times 240 \times V_{i2} = 147.97 V_{i2}$$

$$A_{v2} = 147.97$$

b.  $A_{vT} = A_{v1} A_{v2} = 101.20$

$$A_{v_s} = \frac{Z_{i_1}}{Z_{i_1} + R_s} A_{v_r} = \frac{(10k\Omega)(101.20)}{10k\Omega + 1k\Omega} = 92$$

$$\mathbf{c.} \quad V_i = \frac{Z_{i_2}}{Z_{i_2} + R_s} V_s = \frac{26\Omega}{26\Omega + 1k\Omega} V_s = 0.025V_s$$

$$\text{and } \frac{V_i}{V_s} = 0.025 \quad \text{with } \frac{V_o}{V_i} = 147.97 \quad \text{from above}$$

$$\text{and } A_{v_s} = \frac{V_o}{V_s} = \frac{V_i}{V_s} \cdot \frac{V_o}{V_i} = (0.025)(147.97) = 3.7$$