

Ques. 1.

I - a , II - a , III - c , IV - a

Ques. (2)

Sol<sup>n</sup>: - Advantages of microwave: -

(i) It increases the B.W. availability.

(ii) Directivity increases.

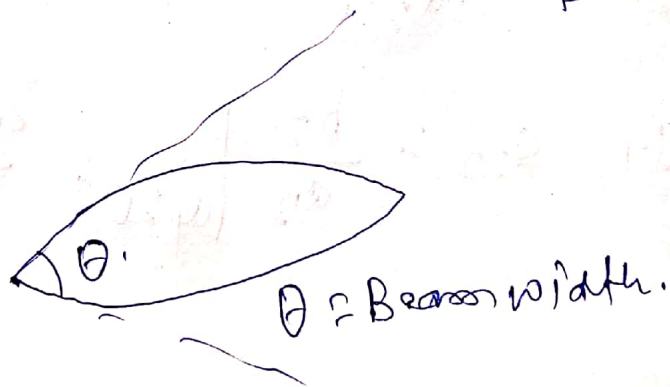
(iii) Size of components decreases.

(iv) Fading effect and Reliability improves.

(v) Transmitter/Receiver power requirements are low at microwave frequency.

(vi) Transparency properties of microwave.

As we know, Directivity  $\propto \frac{1}{\text{Beam width}}$ .

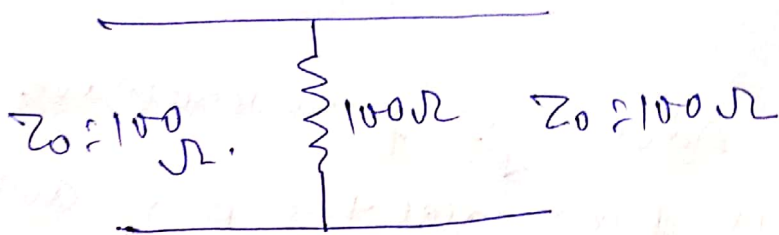


If frequency increases, wavelength ( $\lambda$ ) will decrease.

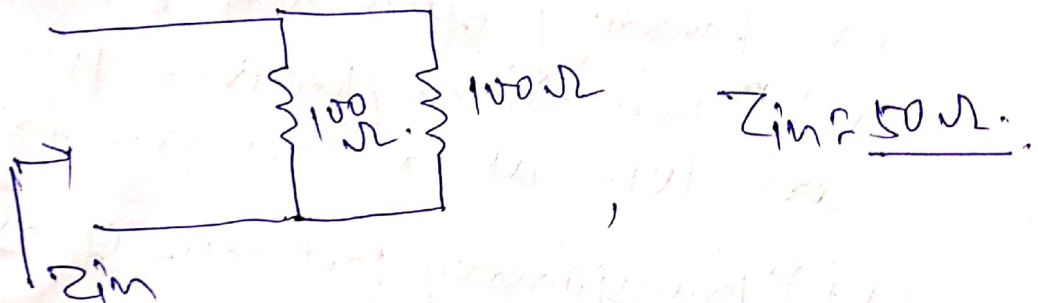
And Beam width is directly proportional to  $\lambda$  so, thus Beam width decreases.

~~and~~  
 $\therefore$  Directivity will increase.

Ques. (B)



To calculate  $S_{11}$ , terminate port 2 in  $100\ \Omega$ .



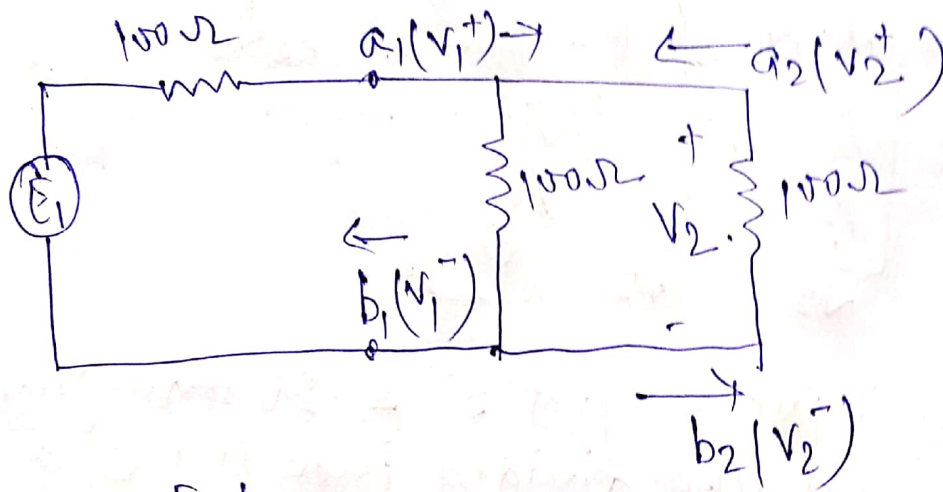
$$S_{11} = \frac{b_1}{a_1} \Big|_{a_2=0} = \frac{Z_{in} - Z_0}{Z_{in} + Z_0} = \frac{50 - 100}{50 + 100} = -\frac{1}{3}$$

Similarly,  $S_{22} = \frac{b_2}{a_2} \Big|_{a_1=0} = \frac{Z_{out} - Z_0}{Z_{out} + Z_0} = -\frac{1}{3}$

$$S_{21} = \frac{b_2}{a_1} \Big|_{a_2=0}$$

Terminate port-2 in  $100\ \Omega$  and drive port ① with  $100\ \Omega$  generator of open circuit voltage  $E_1$





$$S_{21} = \frac{v_2^-}{v_1^+} \Big|_{v_2^+ = 0}, I = \frac{E_1}{Z_0 + Z_{in}}$$

$$v_2 = v_2^- + v_2^+ \quad \therefore \text{Since } v_2^+ = 0, v_2^- = \frac{I}{2} \times Z_0 = 50 I.$$

$$v_1 = v_1^+ + v_1^- = v_1^+ (1 + S_{11})$$

$$Z_{in} I = v_1^+ (1 + S_{11})$$

$$\therefore v_1^+ = \frac{Z_{in}}{(1 + S_{11})} I.$$

$$\therefore S_{21} = \frac{\frac{I}{2} Z_0 (1 + S_{11})}{Z_{in} \cdot I} = \frac{Z_0 (1 + S_{11})}{2 Z_{in}}$$

$$= \frac{100}{2 \times 50} \left(1 - \frac{1}{3}\right) = 1 - \frac{1}{3} = \frac{2}{3}$$

Similarly,  $S_{12} = \frac{2}{3}$

$$\therefore [S] = \begin{bmatrix} -\frac{1}{3} & \frac{2}{3} \\ \frac{2}{3} & -\frac{1}{3} \end{bmatrix} \text{ Ans.}$$



OR.

S-matrix of  $\epsilon$ -plane Tee.

$$S = \begin{bmatrix} 1/2 & 1/2 & 1/\sqrt{2} \\ 1/2 & 1/2 & -1/\sqrt{2} \\ 1/\sqrt{2} & -1/\sqrt{2} & 0 \end{bmatrix}$$

Now, Input to port-3 is 2000W. This power gets equally divided into port-1 and 2  
i.e. at port-1 and port-2, 1000W power will be delivered.

Since port-1 and port-2 have load of 60 $\Omega$  and 75 $\Omega$  respectively. Because of that, there will be reflection and some of the power gets reflected back.

If reflection coefficient at port-1 is  $S_1$  and  $S_2$  at port-2.

Then, power delivered to load 60 $\Omega$  at port-1.

$$\begin{aligned} &= 1000W (1 - S_1^2) \\ &= 10 \left[ 1 - \left( \frac{60-50}{60+50} \right)^2 \right] = 9.92 \text{ mW. Ans.} \end{aligned}$$

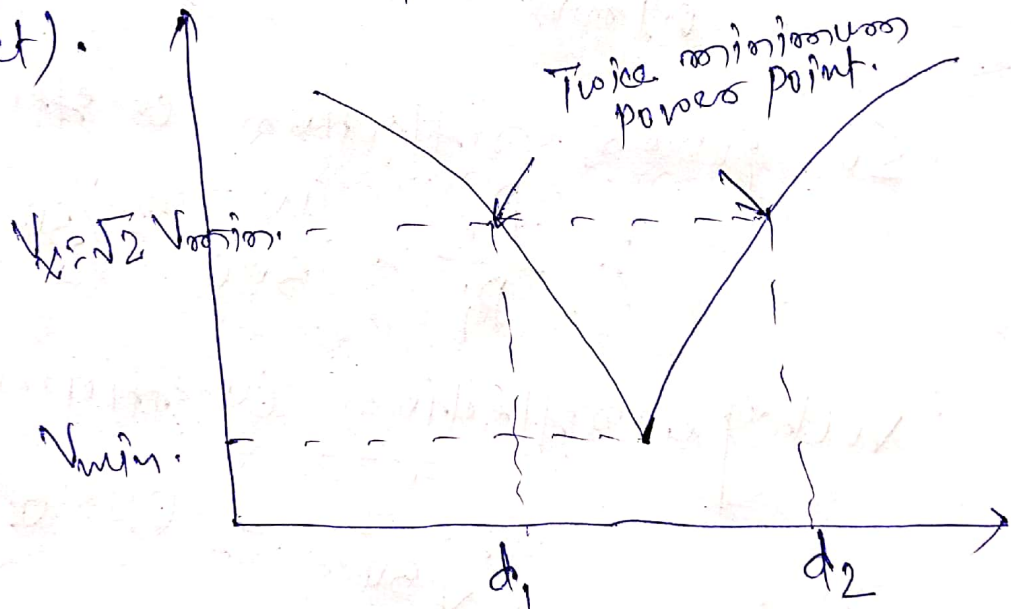
Power delivered to load 75 $\Omega$  at port-2.

$$\begin{aligned} &= 1000W (1 - S_2^2) \\ &= 1000W \left[ 1 - \left( \frac{75-50}{75+50} \right)^2 \right] \\ &= 9.6 \text{ mW. Ans.} \end{aligned}$$

~~Reflected power goes to post~~

Ques. (4) (a)

Sol.  $\rightarrow$  For double minimum method to measure VSWR, the probe is inserted to a depth where the min<sup>m</sup> can be read out without difficulty. The probe is then moved to a point where power is twice the min<sup>m</sup>. Let this position is  $d_1$ . The ~~probe is now~~ twice power point position is  $d_2$  (let).



$$\therefore \frac{2 P_{\min}}{2} \propto V_x^2$$

$$\frac{V_{\min}}{2} = \frac{1}{2}$$

$$V_x = \sqrt{2} V_{\min}$$

Further,  $\lambda_c = 2a$  (for TE<sub>10</sub>)

$$\beta = \frac{\lambda_0}{\sqrt{1 - (\lambda_0/\lambda_c)^2}}$$

$$\text{Then } VSWR = \frac{r_g}{\pi(d_2 - d_1)}$$

(4) (b) Given, Directivity = 20dB  
= 100 (Linear scale)

$$\therefore \frac{P_i}{3000\text{W}} = 100 \Rightarrow P_i = \underline{300000\text{W}}$$

$$\text{Now, } \frac{P_r}{0.1000\text{W}} = 100 \therefore P_r = 10000\text{W}$$

So, power reflection coefficient,  
 $= \frac{P_r}{P_i} = \frac{10}{300} = 1/30$

voltage reflection coefficient,  $= \sqrt{\frac{P_r}{P_i}}$   
 $= \sqrt{\frac{1}{30}} = 0.1816$

$$VSWR = \frac{1 + 0.1816}{1 - 0.1816} = \underline{1.44 \text{ Ans.}}$$



(4) OR.

(a) measurement of impedance:-

(i) measurement of impedance using Reflectometer

(ii) measurement of impedance using slotted line.

(iii) measurement of impedance using magic-T.

(b) Given,  $f = 10 \text{ GHz}$ ,  $a = 4 \text{ cm}$ ,  $b = 2.5 \text{ cm}$ .

$$\lambda_c \text{ (for TE}_{10} \text{ mode)} = 2a = \underline{8 \text{ cm}}$$

$$\lambda_0 = \frac{c}{f} = \frac{3 \times 10^8}{10 \times 10^9} = \underline{3 \text{ cm}}$$

$$d_2 - d_1 = \underline{1 \text{ mm}}$$

we know that  $\Gamma_g = \frac{\lambda_0}{\sqrt{1 - (\lambda_0/\lambda_c)^2}} = \frac{3}{\sqrt{1 - (3/8)^2}}$

$$= \underline{3.236 \text{ cm}}$$

For double minimum method VSWR is given by,

$$\text{VSWR} = \frac{\Gamma_g}{\pi(d_2 - d_1)} = \frac{3.236}{\pi \times 1 \times 10^{-1}} = \underline{10.3}$$

(5) Given,  $V_0 = 20 \text{ kV}$ ,  $I_0 = 2 \text{ amp}$ ,  $f = 8 \text{ GHz}$   
 $\beta_i = \beta_0 = 1$ ,  $S_0 = 10^{-6} \text{ cm}^3$ ,  $V_1 = 10 \text{ V}$  (rms)  
 $R_{in} = 10 \text{ k}\Omega$ ,  $R_{shl} = 30 \text{ k}\Omega$ .

(a) Plasma frequency,  $(\omega_p) = \sqrt{\frac{e S_0}{m \epsilon_0}}$   
 $= \sqrt{\frac{1.7 \times 10^{11}}{8.85 \times 10^{-12}}} \times 10^{-6} = 1.41 \times 10^8 \text{ rad/sec.}$

(b) Reduced Plasma frequency of  $R = 0.15$   
 $\omega_q = R \omega_p = 0.705 \times 10^8 \text{ rad/sec.}$

(c) Produced current in Output cavity  
 $(I_{2ind}) = \frac{1}{2} \beta_0^2 \left( \frac{\omega}{\omega_q} \right) \cdot \frac{I_0}{V_0} |V_1|$   
 $= \frac{1}{2} \times 1 \times \left( \frac{2\pi \times 8 \times 10^9}{0.705 \times 10^8} \right) \times \left( \frac{2}{20 \times 10^3} \right) \times 10 \text{ V}$   
 $= 0.3565 \text{ Amp.}$

(d) Produced voltage in output cavity,  
 $V_{2ind} = I_{2ind} \cdot R_{shl} = 0.3565 \times 30$   
 $= 10.69 \text{ kV}$

(e) Output power delivered to the load.  
 $= I_{2ind}^2 R_{shl} = (0.3565)^2 \times 30 = 3.82 \text{ kW.}$



5 OR.

Given,  $N = 10$ ,  $f = 300 \text{ Hz}$ ,  $a = 0.4 \text{ cm}$ ,  $b = 0.9 \text{ cm}$   
 $l = 2.5 \text{ cm}$  (anode length)  
 $V_0 = 18 \text{ kV}$ ,  $B = 0.2 \text{ wb/m}^2$ .

(a) Angular velocity of electron

$$\omega = \frac{Bq}{m} = \frac{0.2 \times 1.6 \times 10^{-19}}{9.1 \times 10^{-31}}$$

$$= 0.2 \times 1.759 \times 10^{11}$$

$$= 5.9 \cdot 3518 \times 10^{10} \text{ rad/sec.}$$

(b) Since the magnetic field is necessary to ~~maintain~~ motion of  $e^-$  ~~travel in a~~  $e^-$  travel in a cycloidal path, then output centrifugal force is equal to pulling force.

$$\frac{mv^2}{R} = Bqv$$

$$\frac{v}{R} = \frac{Bq}{m}$$

$$R = \frac{mv}{Bq} = v/\omega$$

$$\text{Now, } v = 0.593 \times 10^6 \sqrt{V_0} = 0.593 \times 10^6 \times \sqrt{18 \times 10^3}$$
$$= 79.55 \times 10^6$$

$$\therefore R = 79.55 \times 10^6 / 0.3518 \times 10^{11} = 2.26 \text{ cm.}$$